

0.0.1 One-way Model

Let y_{ik} denote the score from the i th subject in response to the k th item ($1 \leq i \leq n, 1 \leq k \leq K$). Consider modeling y_{ik} using a single-factor, linear random-effect model:

$$\begin{aligned} y_{ik} &= \mu + \beta_i + \epsilon_{ik}, & \beta_i &\sim N(0, \sigma_\beta^2), & \epsilon_{ik} &\sim N(0, \sigma^2), & \beta_i &\perp \epsilon_{ik} \\ 1 &\leq k \leq K, & 1 &\leq i \leq n. \end{aligned}$$

The ICC in this model is $\rho = \frac{\sigma_\beta^2}{\sigma_\beta^2 + \sigma^2}$ based on the linear mixed effect model. In this R function we used a distribution-free alternative to provide robust inference of ICC based on the theory of U-statistics.